



## Free Standing Mathematics Qualification

# Working with Algebraic and Graphical Techniques

## 6991/2

# Mark Scheme

## *2005 examination – June series*

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

**Free-Standing Mathematics Qualification**

**Advanced Level: Working with Algebraic & Graphical Techniques (6991/2)**

**June 2005**

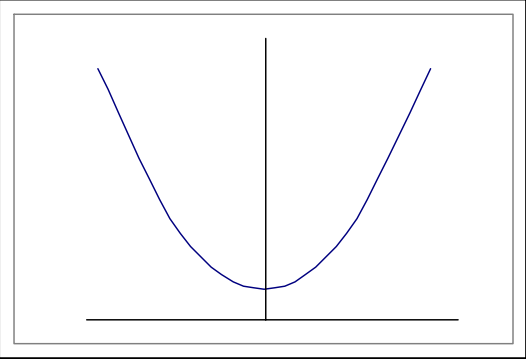
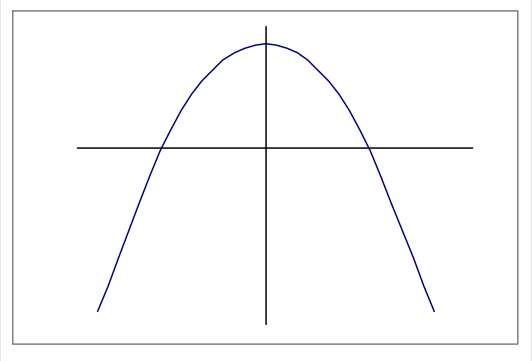
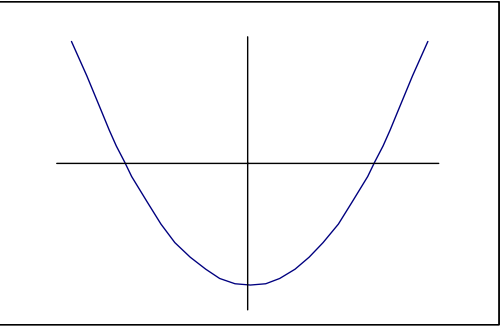
**Question 1**

(a)	7 correct plots (0,0) (5,250) (10,400) (15,450) (20,400) (25,250) (30,0) to $\frac{1}{2}$ square accuracy smooth correct curve	B3   B1	5 correct B2   4 correct B1
(b)(i)	450m <sup>2</sup>	B1	
(ii)	15m	B1	
(c)	attempt to find both sides 60	M1 A1	
(d)	$q = 15$ $p - 2q^2 = 0$ $p = 450$	B1 M1 A1	oe
(e)	$q$ gives $x$ value for max $p$ gives max area	B1 B1	
	<b>TOTAL</b>	<b>13</b>	

**Question 2**

(a)	9 correct plots (0,7) ( $\pm 5$ , 7.26) ( $\pm 10$ , 8.09) ( $\pm 15$ , 9.7) ( $\pm 20$ , 12.5) to $\frac{1}{2}$ sq. accuracy smooth correct curve	B3   B1	B2 for 6 correct B1 for 4 correct
(b)	7m	B1ft	or ft provided U-shaped curve
(c)	$x = \pm 20$ 12.5 ft their curve provided U-shaped	M1 A1ft	
	<b>TOTAL</b>	<b>7</b>	

**Question 3**

	<p>correct curvature and correct crossing of vertical axis and all 3 graphs must be symmetrical about y- axis. No curve to go through (0,0).</p> <p><math>y = P + Qx^2</math></p>  <p><math>y = P - Qx^2</math></p>  <p><math>y = Qx^2 - P</math></p>  <p><math>Y = P + Qx^2</math> is best</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p>	
	<p><b>TOTAL</b></p>	<p><b>4</b></p>	

**Question 4**

(a)(i)	$\ln T = \ln(Ae^{-kx})$ $\ln T = \ln A - kx$	M1 A1	
(ii)	4.50, 4.25, 4.00, 3.75, 3.50, 3.25, 3.00	B2	-1 if use log B1 for 4 correct
(iii)	correct plots to $\frac{1}{2}$ sq. accuracy line through points	B2 B1	B1 for 4 correct line of best fit
(iv)	$A = 88$ to $92$ $k =$ gradient and attempt seen $k = 0.045$ to $0.055$	B1 M1 A1	
(b)(i)	initial temperature	B1	highest possible temp.
(ii)	sub $x = 10$ $52.1$ °C	M1 A1	
(iii)	$30/95 = e^{-0.06x}$ $\ln(30/95) = -0.06x$ 19 to 19.5 mins	M1 M1 A1	$\ln 30 = \ln 95 - 0.06x$ $\ln 30 - \ln 95 = -0.06x$
(iv)	$x$ gets large $T$ tends to $0$ °C	B1	
	<b>TOTAL</b>	<b>17</b>	

**Question 5**

(a)(i)	$h = 18$ hours $t = 180$ days	B1 B1	
(ii)	68.5 to 72.5 287.5 to 291.5	B1 B1	
(b)(i)	tangent drawn at $t = 120$ 0.07 to 0.11	M1 A1	
(ii)	rate of change of hours of daylight hours per day	B1 B1	oe
(c)	$132 \pm 2$ or $228 \pm 2$ $96 \pm 3$	M1 A1	
(d)	10.4 to 10.45 $(10.6 - \text{their } 10.45) / 10.6 \times 100$ 1.4% to 1.9%	B1 M1 A1	allow $\pm$
(e)	$t(x)$ translate $+90^\circ$ stretch parallel to $h(y)$ axis scale factor 6 $h(y)$ translate $+12$	B1  B1 B1	
(f)	amplitude 6 period 360	B1 B1	
(g)	$A = 5$	B1	
	<b>TOTAL</b>	<b>19</b>	
	<b>TOTAL FOR PAPER</b>	<b>60</b>	